

# Physics 142 - October 23, 2007

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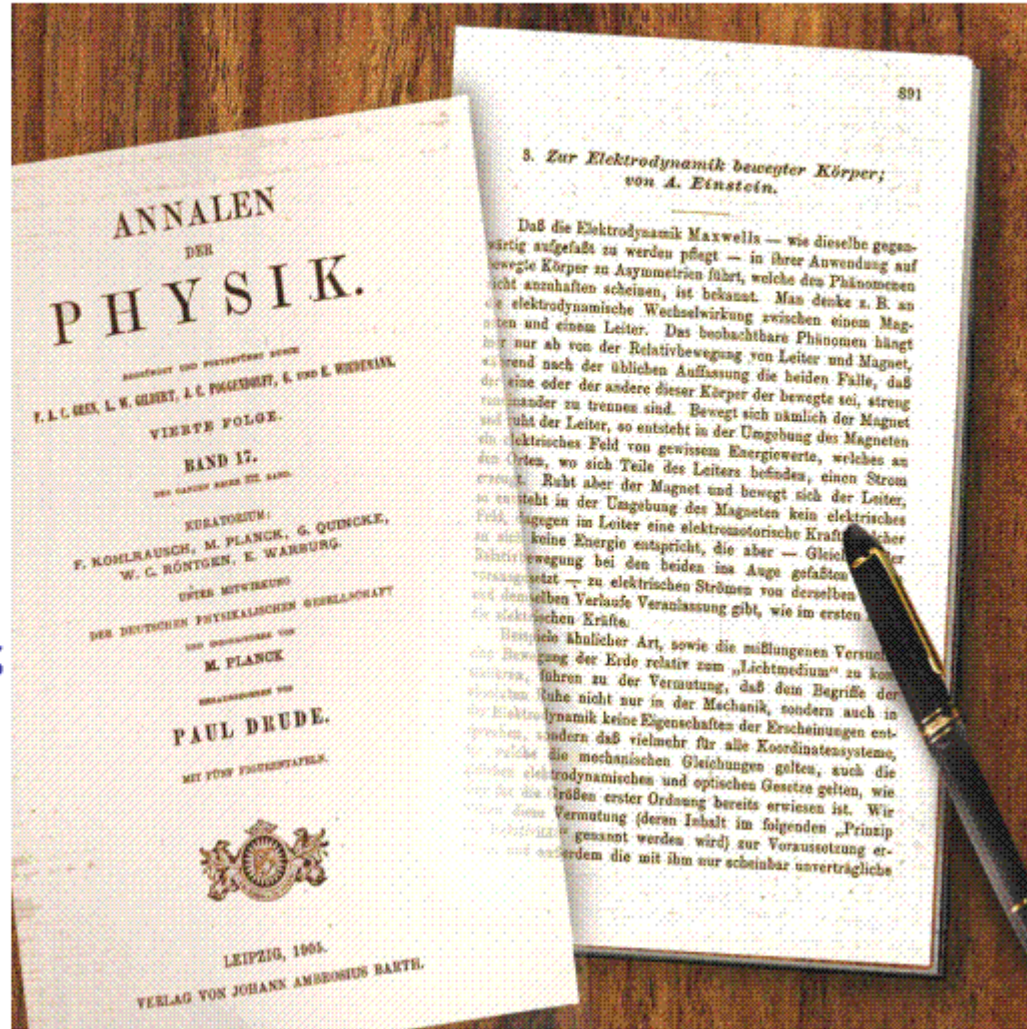
- Be sure to listen to accompanying Audio file for this lecture
- Let me know about technical difficulties
- Please e-mail me with questions
- I will assume you have covered this material (prob sets, workshops, future lectures)
- Presentation groups posted on web

Last Time

Einstein's  
1905 paper  
on Special  
Relativity

"On the Electrodynamics  
of Moving Bodies"

Was a great year  
for AI



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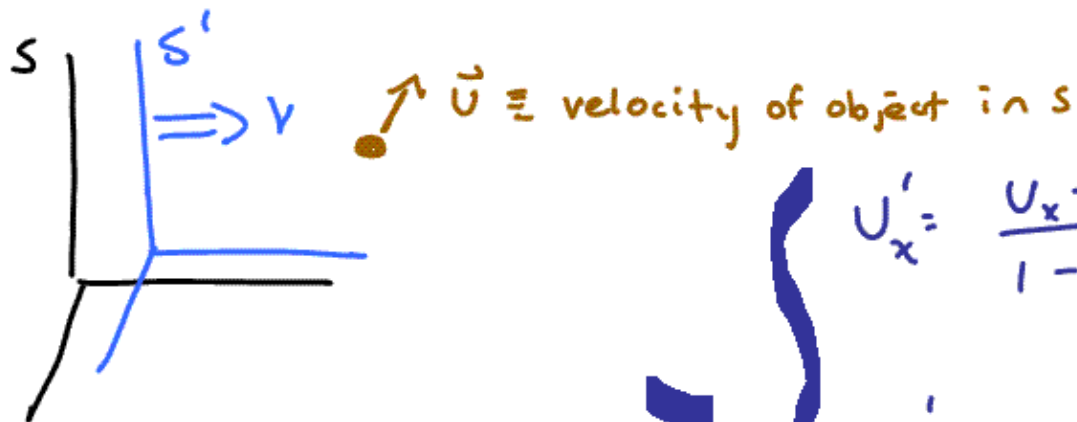
Lorentz Transformations

$$x' = \gamma(x - vt)$$

$$y' = y$$

$$z' = z$$

$$t' = \gamma\left(t - \frac{vx}{c^2}\right)$$



Relativistic  
velocity  
Transformation

$$U'_x = \frac{U_x - v}{1 - \frac{v}{c^2}U_x}$$

$$U'_y = \frac{U_y}{\gamma\left(1 - \frac{U_x v}{c^2}\right)}$$

$$U'_z = \frac{U_z}{\gamma\left(1 - \frac{U_x v}{c^2}\right)}$$

proper time  $\equiv \tau$  - Time measured in rest frame of event <sup>4</sup>

define proper velocity  $\eta = \frac{dx}{d\tau} = \gamma \frac{dx}{dt} = \gamma v$

Spacetime "4-vector"

$x, y, z, t$

Energy-Momentum "4-vector"

define  $p = m\eta = m\gamma v$

$p_x, p_y, p_z, E$

$E \equiv \gamma mc^2$

$E, P$  Lorentz transforms just like  $x, t$

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$$x' = \gamma(x - vt)$$

$$y' = y$$

$$z' = z$$

$$t' = \gamma\left(t - \frac{vx}{c^2}\right)$$

$$P_x' = \gamma(P_x - vE)$$

$$P_y' = P_y$$

$$P_z' = P_z$$

$$E' = \gamma\left(E - \frac{vP_x}{c^2}\right)$$

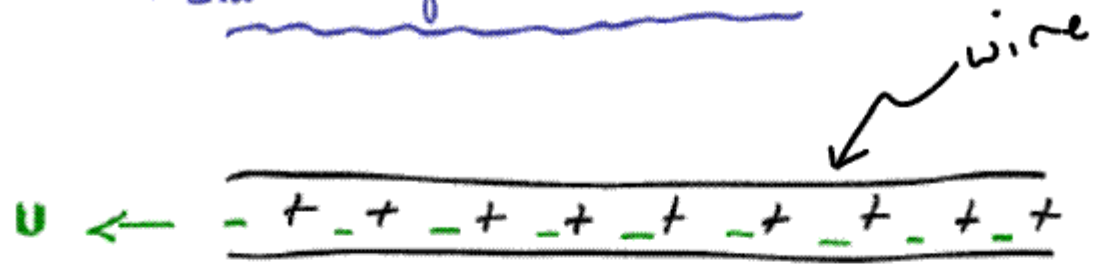
$$E = mc^2 + \frac{1}{2}mv^2 + \text{h.o.t.}$$

↑  
Relativistic  
Energy

↑  
 $m$   
"rest  
mass"  
(CONSTANT)

↑  
Kinetic  
Energy

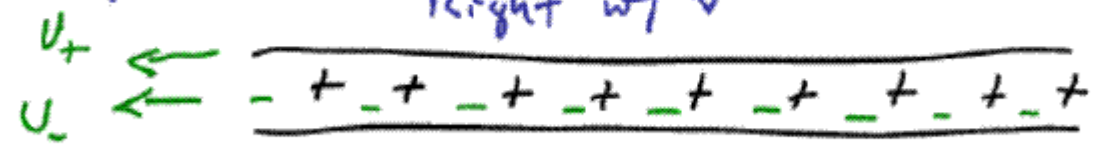
# Relativity and E+M



$$\lambda_- \approx \lambda_+$$

(A)  $g_0$  no NET  $\vec{E}$ , No force

go to reference frame where you are moving Right w/ v



$$|u_-| > |u_+|$$

$$\lambda_- \neq \lambda_+$$

$u_+$  ←  $g_0$  now you will see an Electric force

due to perceived different  $\lambda$ 's

... or is it a magnetic force? 7

# Magnetism

Magnetic field  $\equiv \vec{B}$

MKS units  
Tesla

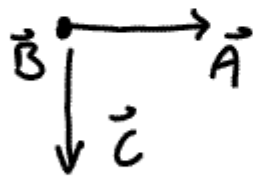
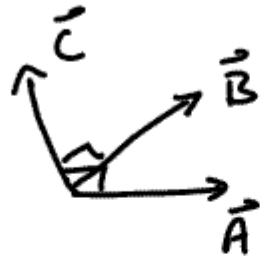
Lorentz Force law

$$\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$$

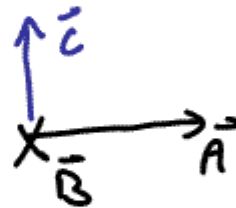
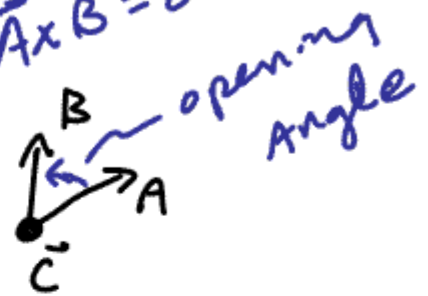
Force on charged particle  
moving w/ velocity  $\vec{v}$  in  
region of electric field  $\vec{E}$   
and magnetic field  $\vec{B}$

## Cross product review

use  
Right hand rule



evaluate direction  
of  $\vec{A} \times \vec{B} = \vec{C}$

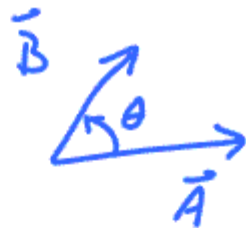


See link for video of how to find direction  
of cross product using right hand rule

<http://physics.syr.edu/courses/video/RightHandRule/index2.html>



$$|\vec{A} \times \vec{B}| = |\vec{A}| |\vec{B}| \sin \theta$$



can evaluate as Determinant

opening Angle between vectors  $\vec{A}$  and  $\vec{B}$

(A)  $\vec{A} \times \vec{B} = \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ A_x & A_y & A_z \\ B_x & B_y & B_z \end{vmatrix} = \hat{i}(A_y B_z - A_z B_y) - \hat{j}(A_x B_z - A_z B_x) + \hat{k}(A_x B_y - A_y B_x)$

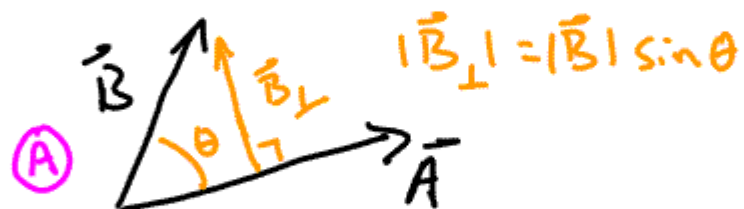
(B)  $\begin{vmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{vmatrix}$

(C)  $\begin{vmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{vmatrix}$

The diagram shows the expansion of the determinant in (A) and the corresponding terms in (B) and (C). Arrows indicate the mapping from the terms in the determinant to the terms in the expansion. A red cloud-like shape encloses the expansion result.

█ Cross product is a vector

█ Cross product magnitude is product of magnitude of one vector and  $\perp$  component of the other vector

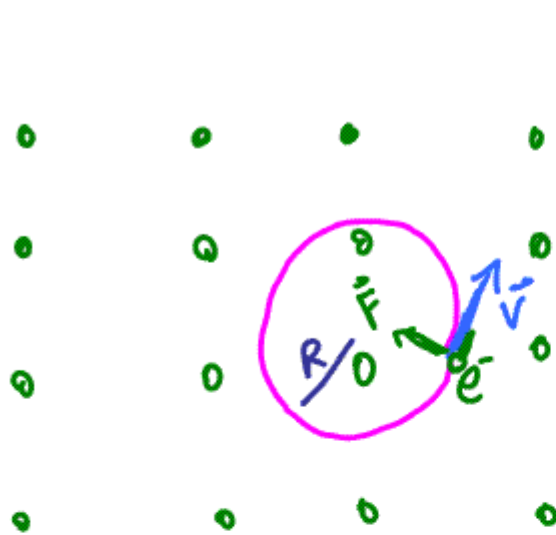


magnetic part of Lorentz force is at right angles to  $\vec{v}$  and  $\vec{B}$   $\rightarrow q\vec{v} \times \vec{B}$



$$\vec{F} = 0$$

no magnetic force if  $\vec{v} = 0$  or  $\vec{v} \perp \vec{B}$



Region of uniform  $\vec{B}$   
out of screen

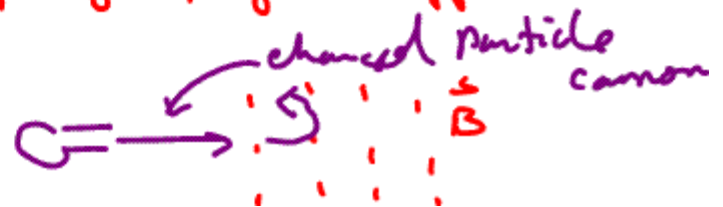
$$\vec{F}_{\text{Magnetic}} = \text{centripetal force}$$

$$\textcircled{A} \quad F_c = \frac{mv^2}{R} = qvB$$

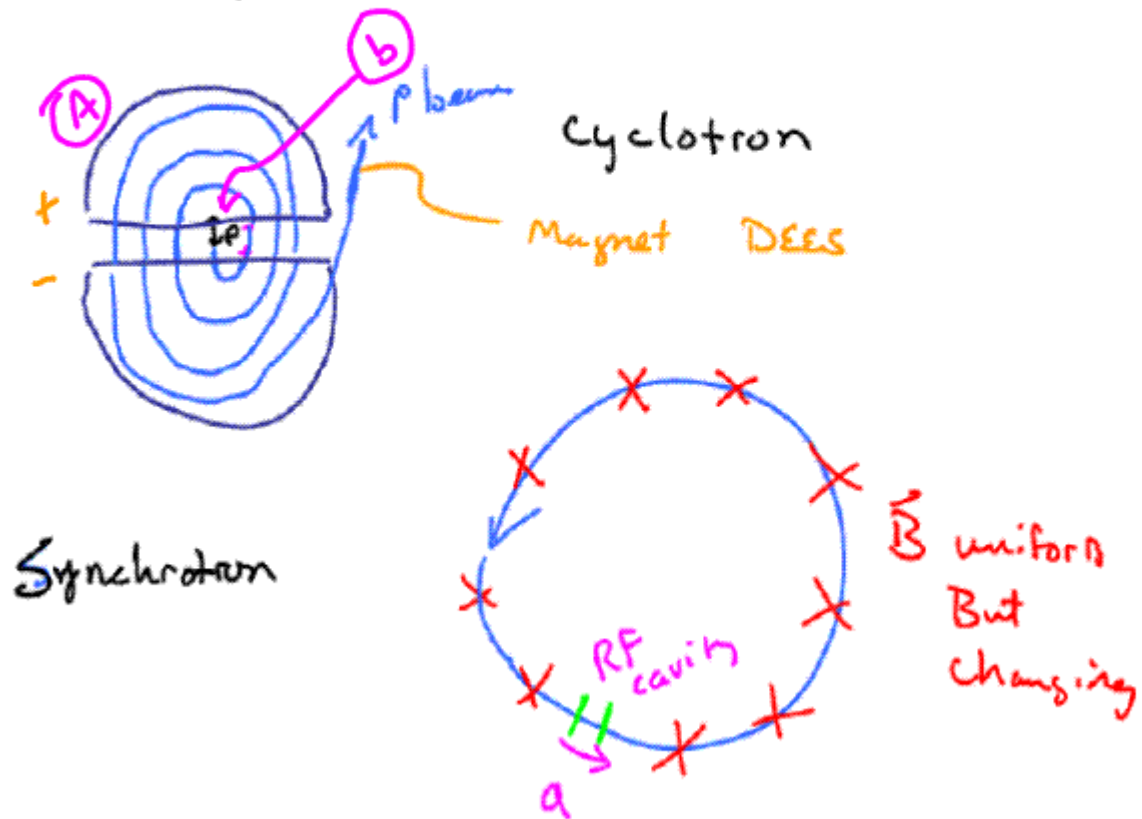
$$R = \frac{mv}{qB} \quad \textcircled{B}$$

magnetic fields commonly used to control path  
of charged particles

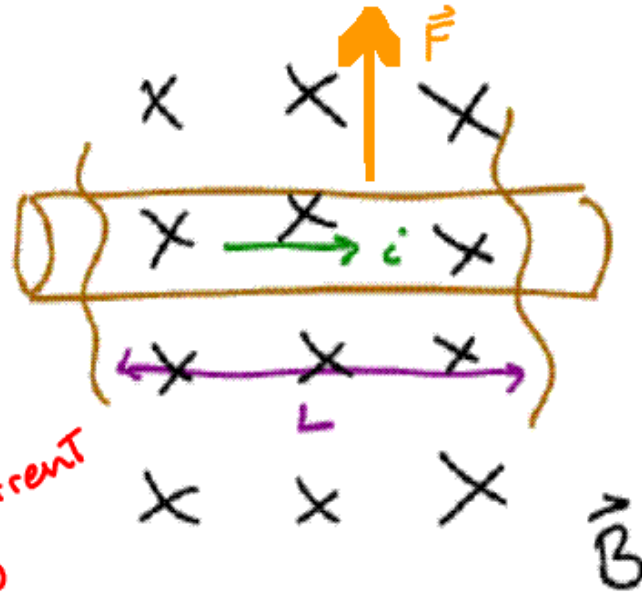
Go to class website and play w/ java applet  
"magnetic fields"



# Particle Accelerators



Current in a wire  $\Rightarrow$  moving charges 13



Remember direction of  $i$  is that for  $\oplus$  current flow

$\Downarrow$   
expect magnetic force on current-carrying wires.

(A) 
$$\vec{F}_{\text{wire}} = (q \vec{v}_d \times \vec{B}) n A L$$

Annotations:  
 -  $q \vec{v}_d$ : charge dr. ft velocity  
 -  $n$ : #charges unit volume  
 -  $A$ : x-sectional area  
 -  $L$ : length

(B) 
$$i = n q v_d A$$

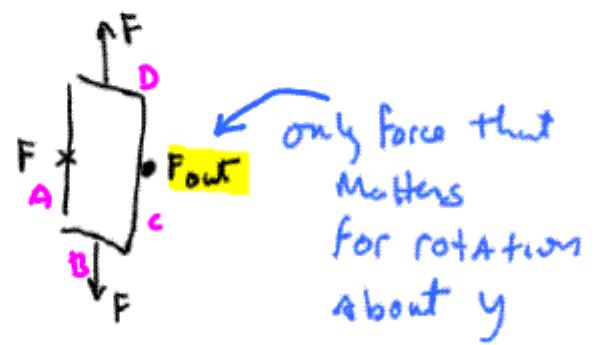
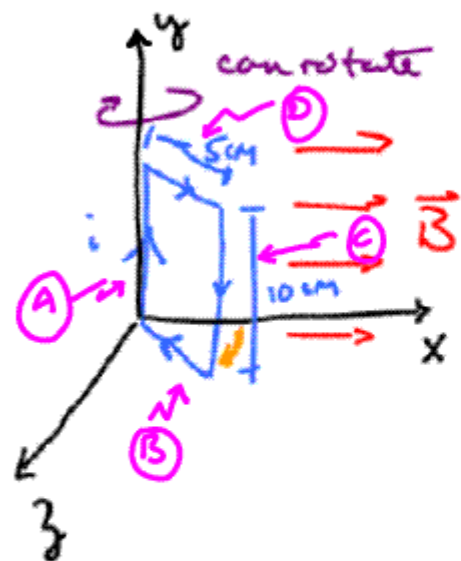
$$\vec{L} = L (\hat{i} \text{ direction})$$

(C) 
$$\vec{F}_{\text{wire}} = L \hat{i} \times \vec{B} \quad \text{or} \quad i \vec{L} \times \vec{B}$$

Current loop in  $\vec{B}$  - what is torque about y axis?

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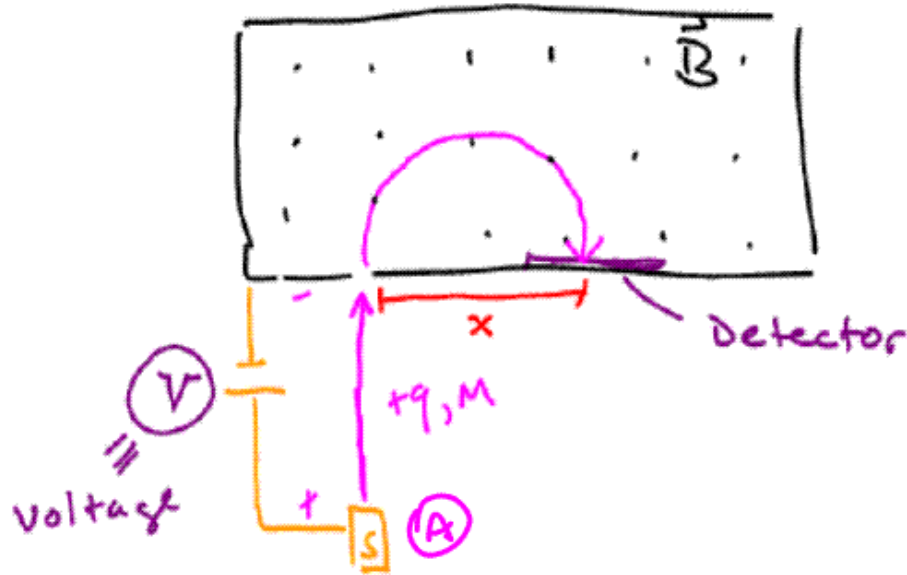
observe from this pt of view  $\rightarrow$  Project in x-z plane



$$\vec{\tau} = F \cos \theta r (\text{down } -\hat{y})$$

$$i l B$$

# Mass Spectrometer



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See Magnetic fields java applet on class website

$$F = qvB \quad F = \frac{mv^2}{R}$$

v = velocity

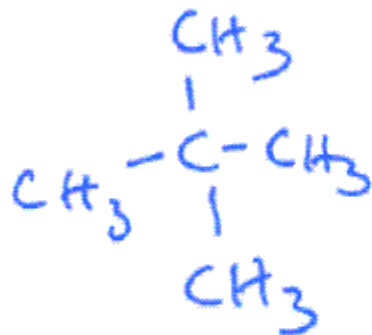
$$qvB = \frac{mv^2}{R} \quad m = \frac{qRB}{v}$$

$$KE = +q|e|V = \frac{1}{2}mv^2$$

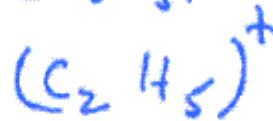
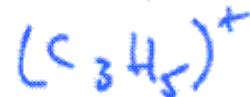
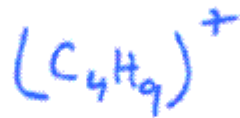
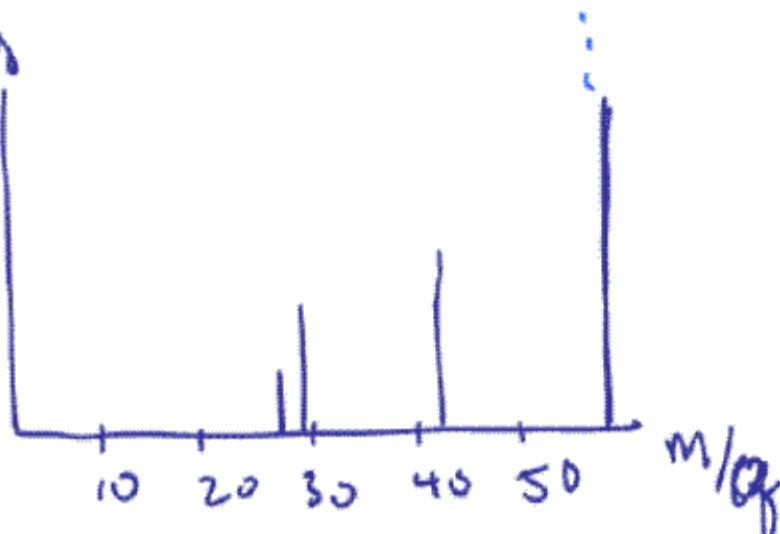
$$v = \left( \frac{2qV}{m} \right)^{1/2}$$

$$x = 2R$$

$$(A) m = \frac{16q^2 R^2 B^2}{2V} = \frac{16q^2 B^2 x^2}{8V}$$



Relative  
Intensity



$m/q$

57

41

29

⋮

Rel. int.

100

41.5

38.5

⋮

$\frac{m}{q}$  determined  
by  $x$   
position