

Physics 142 - Sept. 4, 2007

recall what you know about the most obvious force of nature  $\rightarrow$  gravitation

$$6.67 \times 10^{-11} \frac{\text{N} \cdot \text{m}^2}{\text{kg}^2}$$

$$|\vec{F}| = \frac{G M_1 M_2}{r^2}$$



one "charge"  
 $\hookrightarrow$  mass

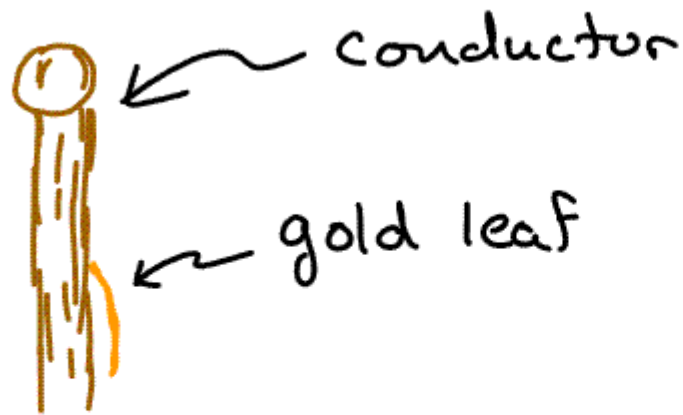
$\hat{r}$  = unit vector along  $\vec{r}$

Force is only Attractive

$$\vec{F} = - \frac{G M_1 M_2}{r^2} \hat{r}$$

"-" sign  
 $\hookrightarrow$  Attractive force

# Electric charge + Electroscopes



Lucite rod  
rubbed w silk



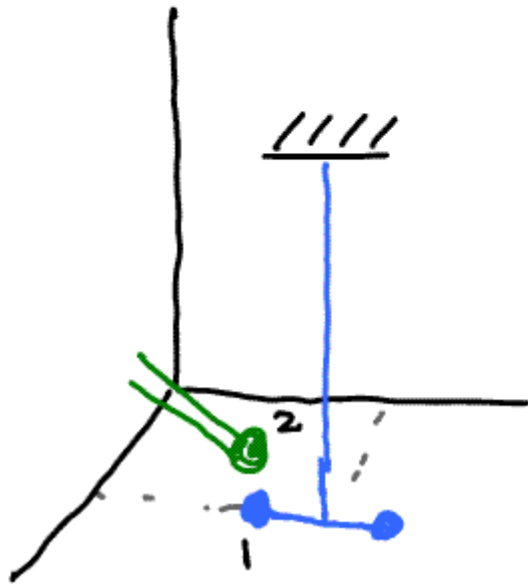
Vice versa we start w other rod

# Electric charge

Two types

like types repel  
unlike types attract

Charles Augustin Coulomb 1785 (1736-1806)



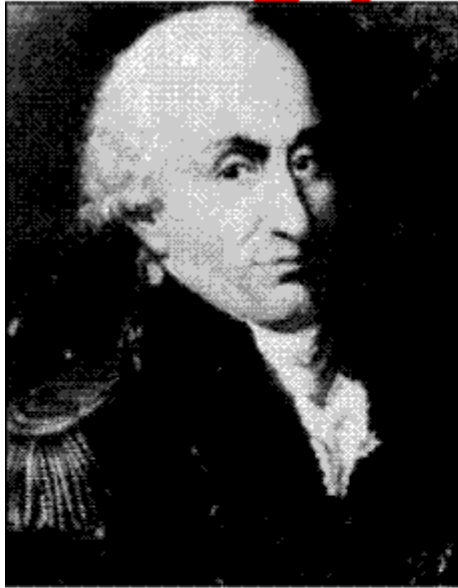
Torsion balance

Studied force as fn  
of charge + DISTANCE

$$F \propto \frac{q_1 q_2}{r^2}$$

Coulomb's  
LAW

# Electric force



Charles Coulomb  
(1736-1806)

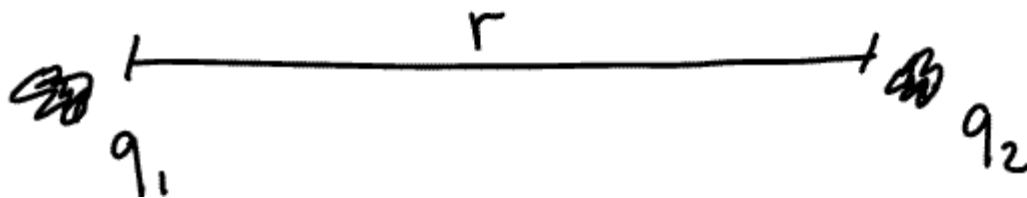
French military engineer

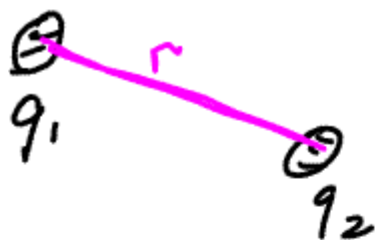
⇒ Coulomb's Law

$$F_{\text{electric force}} = k \frac{q_1 q_2}{r^2}$$

$q \equiv$  electric charge

$$q_{1,2} = \pm \#$$





$$\vec{F}_{12} = \frac{k q_1 q_2 \hat{r}}{r^2}$$

Force of  $q_1$  on  $q_2$

Vector

$\hat{r}$  unit vector along  $\vec{r}$

$k$  constant = sets the scale

$$\left\{ \begin{array}{l} \frac{1}{4\pi\epsilon_0} \\ 8.99 \times 10^9 \frac{\text{N}\cdot\text{m}^2}{\text{C}^2} \end{array} \right. \vec{F} = \frac{1}{4\pi\epsilon_0} \frac{q_1 q_2 \hat{r}}{r^2}$$

MKS units

$F$  in Newtons

$r$  in m

$q$  in Coulombs

$$\epsilon_0 = 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{N}\cdot\text{m}^2}$$

Permittivity of free space

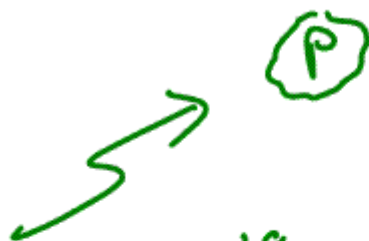
electric charge is conserved

electric charge is quantized

$$\pm |e| = 1.6 \times 10^{-19} \text{ Coulombs}$$

$$\left. \begin{array}{l} |q| = \frac{2}{3} \\ \quad = \frac{1}{3} \end{array} \right\} \text{quarks}$$

H atom



$$Q = 1.6 \times 10^{-19} \text{ Coulombs} \\ = +1|e| \quad C$$

Charge is quantized



Bohr Atom

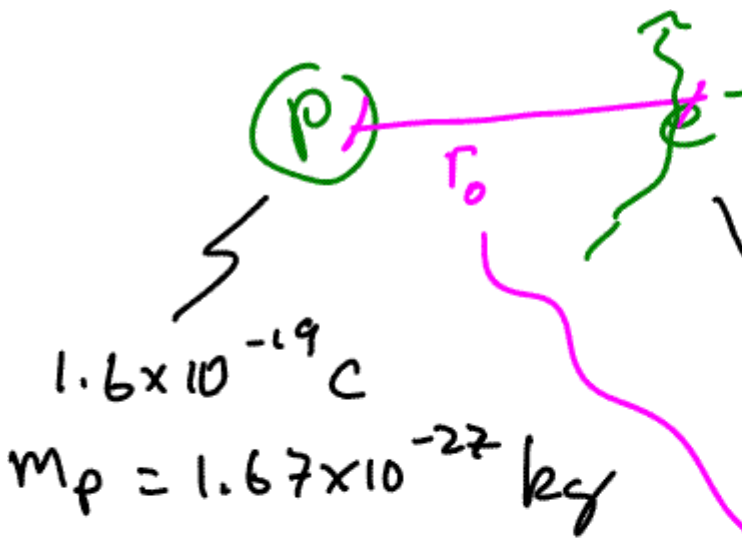
$e^-$  moves in a circle  
abt the proton  
Proton is stationary

$$Q = -1.6 \times 10^{-19} C \\ = -1|e|$$

$$1.6 \times 10^{-19} C \equiv e \\ |e|$$

only integral charge (multiples of  $|e|$ ) found in nature.

Quarks - which are constituents of particles like protons - have fractional charge but are not seen in nature because they are confined by the strong nuclear force.



How does  $F_{em}$  compare to  $F_{gravity}$ ?

Electrostatic

$m_e = 9.11 \times 10^{-31} \text{ kg}$

$r_0 \equiv \text{Bohr radius} = 5.29 \times 10^{-11} \text{ m}$

$$F_{em} = \frac{k q_1 q_2}{r^2} = \frac{8.99 \times 10^9 \frac{\text{N m}^2}{\text{C}^2} (1.6 \times 10^{-19} \text{ C})^2}{(5.29 \times 10^{-11} \text{ m})^2}$$

$$F_{em} = 8.2 \times 10^{-8} \text{ N}$$



$$|F_{\text{grav}}| = \left| -G \frac{M_p m_e}{r^2} \right| = 3.6 \times 10^{-47} \text{ N}$$

$$\frac{F_{\text{em}}}{F_{\text{grav}}} = 2.3 \times 10^{39}$$

(b) What is the speed of  $e^-$ ?

$$F_{\text{centrifugal}} = F_{\text{em}} = \frac{m_e v_e^2}{r_0}$$

$$v_e = 2.2 \times 10^6 \text{ m/s} \sim 1\% \text{ speed of light}$$