

Physics 114 - February 14, 2006

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Exam I  
in ① week  
→ here



questions? issues?

Last Time - Energy + Potential  
in Electrostatics

$$\text{Potential difference} = W/q$$

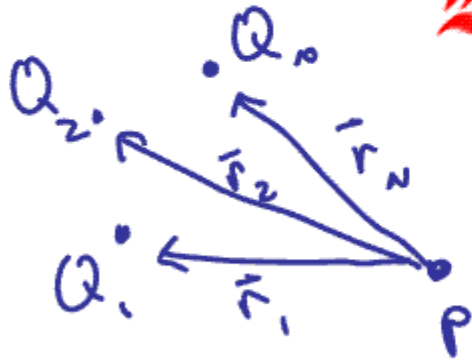
in units of Volts  $\equiv$  J/C

**→**  $V_{\text{pt chg}} = \frac{kQ}{r}$  where  $V \rightarrow 0$  at  $\infty$



Potential is a scalar quantity

**Important**



$$V_P = \sum \frac{kQ_i}{r_i}$$



$$V_P = \int_{\text{vol}} \frac{k dQ}{r}$$



Electric potential is path independent

Electric force is conservative

$$\vec{E} = 0 \quad \text{in Conductor}$$



Conductor is  
all at same  
potential

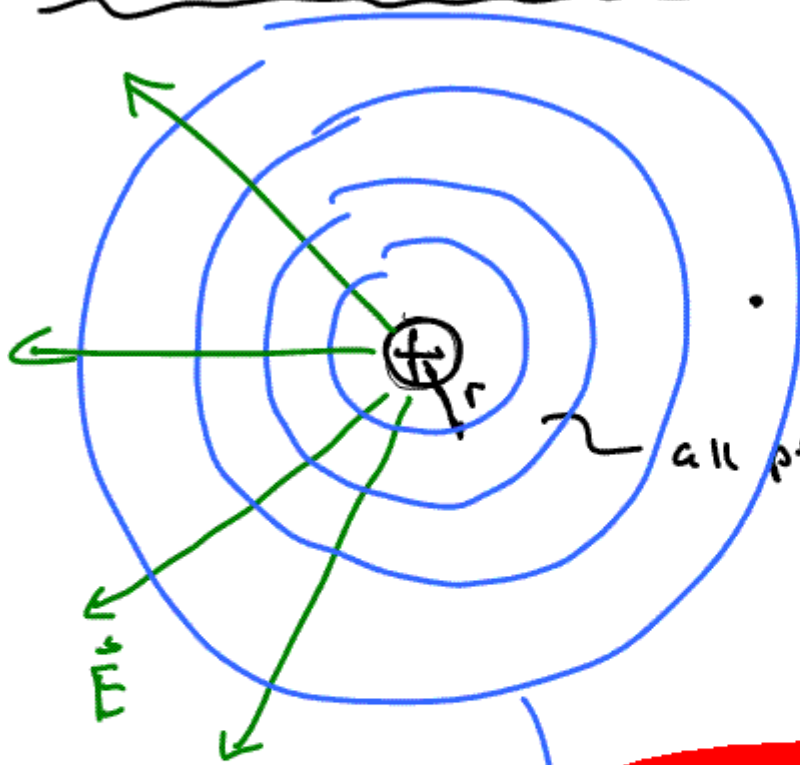
Equipotential

Can Get  $\vec{E}$  from  $V$

$$\vec{E}_s = - \frac{dV}{ds}$$

# Equipotential lines

$$V_p = \frac{kQ}{r}$$

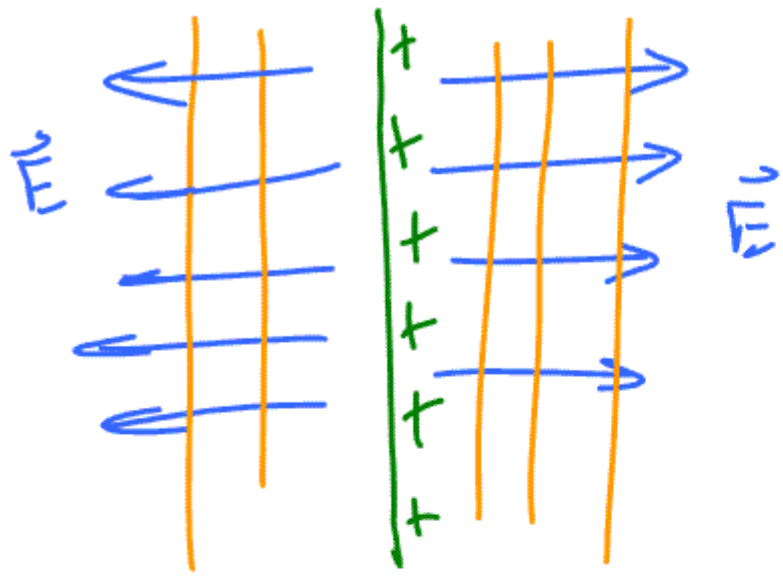


all pts at same  $r$   
have same potential

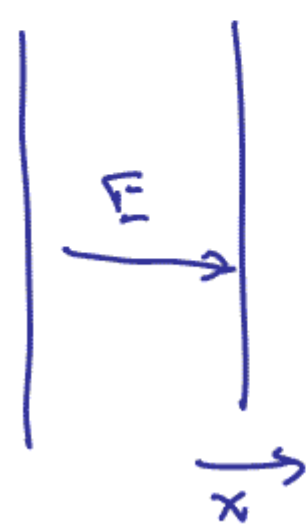
Equipotential lines  
⊥  $\vec{E}$

$$E = -\frac{dV}{dr}$$

$\infty$  plane of charge

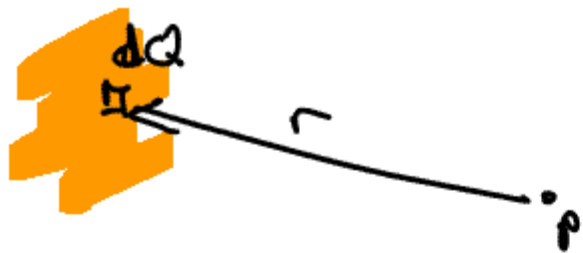


lines of equipotential

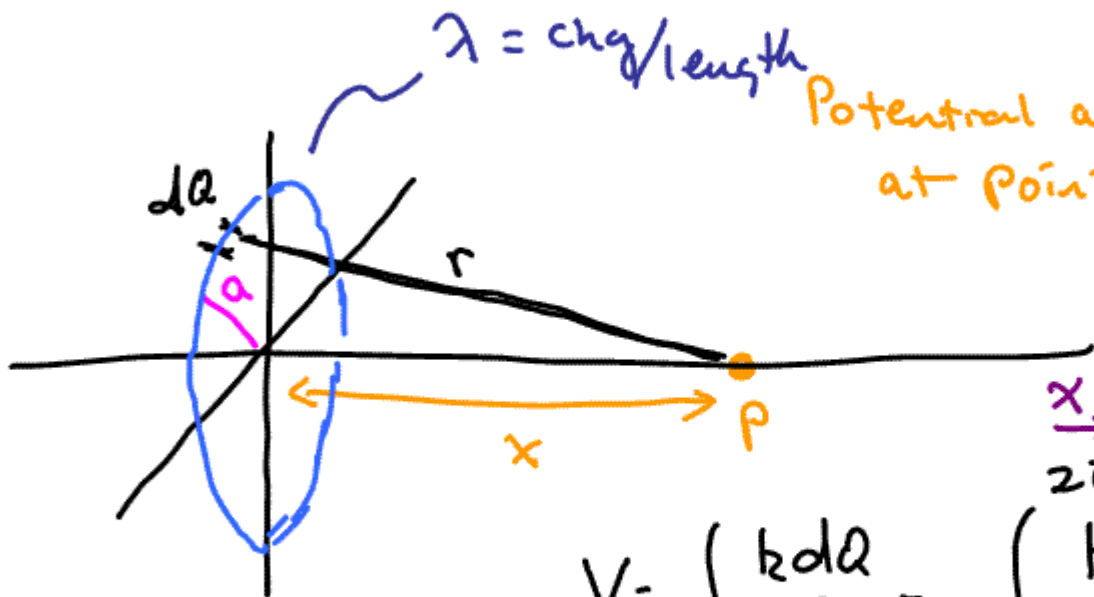


$$E_x = -\frac{dV}{dx}$$





$$V_P = \int \frac{k dQ}{r}$$



$\lambda = \text{chg/length}$

Potential at P?  
at point x on x-axis

$$dQ = \lambda ds$$

$$V = \int \frac{k dQ}{r} = \int_0^{2\pi a} \frac{k \lambda ds}{r}$$

$$V_P = \frac{k \lambda}{\sqrt{x^2 + a^2}} \int_0^{2\pi a} ds = \frac{k \lambda 2\pi a}{\sqrt{x^2 + a^2}}$$

$$\frac{dv}{dx} = -k\lambda 2\pi a \frac{1}{2} (x^2+a^2)^{-3/2} 2x$$

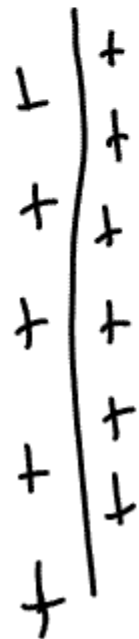
$$E_x = -\frac{dv}{dx} = + \frac{k\lambda 2\pi a x}{(x^2+a^2)^{3/2}}$$

units go as  
 $\frac{kQ}{r^2}$  okay ✓

I dropped this x  
 during lecture  
 - fix your notes

$V_p$   $x \gg a$

chg density  $\equiv \sigma$  as plane



$$\oint \vec{E} \cdot d\vec{A} = \frac{Q_{encl}}{\epsilon_0}$$

$\int + \int + \int$

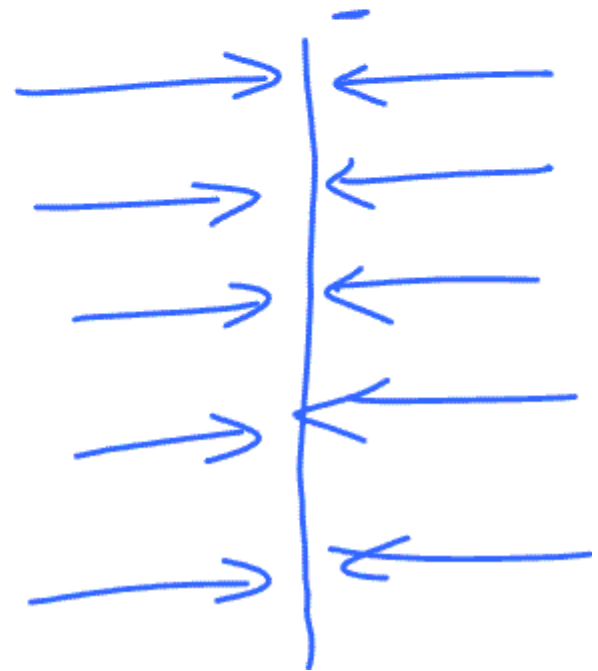
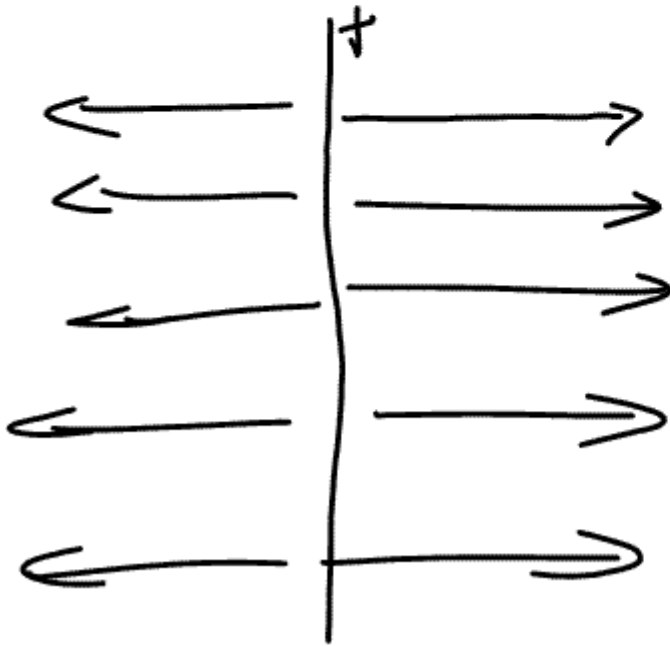


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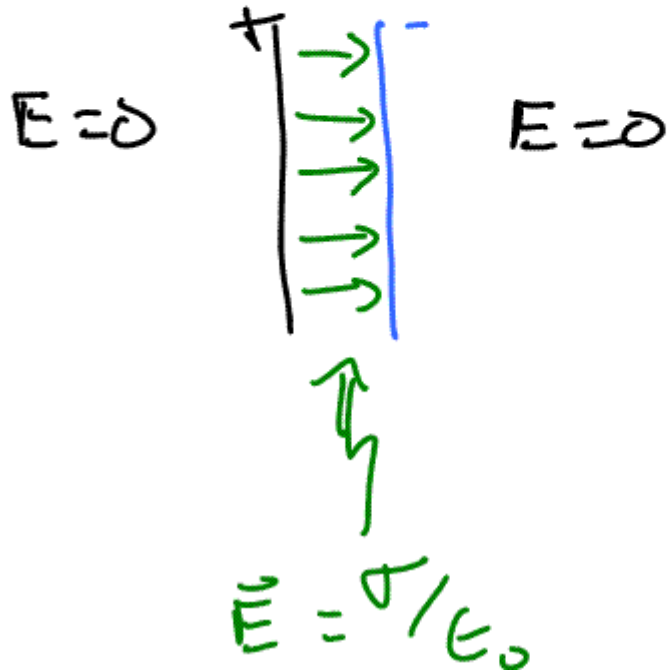
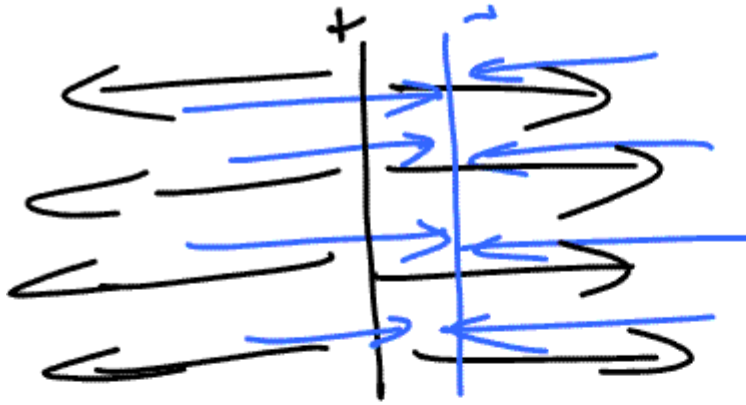
$$\oint \mathbf{E} \cdot d\mathbf{A} = 2|\mathbf{E}|A = \frac{Q_{\text{encl}}}{\epsilon_0} = \sigma A$$

$$2|\mathbf{E}|A = \frac{\sigma A}{\epsilon_0}$$

$$|\mathbf{E}| = \frac{\sigma}{2\epsilon_0}$$







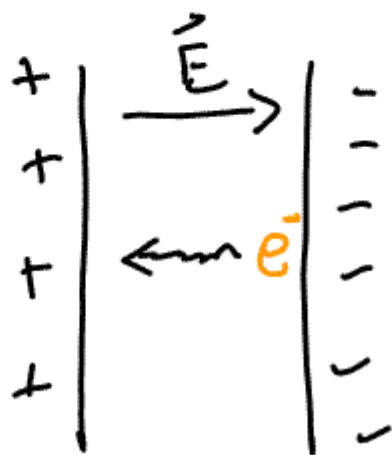
Parallel  
plates



$$V_{\text{bet plates}} = - \int \vec{E} \cdot d\vec{s} = -|E|d$$

$$\Delta V = |E|d = \frac{\sigma}{\epsilon_0} d$$

$$\Delta V = 1 \text{ Volt}$$



How much  
Energy  
is  
gained  
by  $e^-$

$$\text{Pot diff} = \frac{\text{Work}}{\text{Charge}} \quad \begin{array}{l} \text{Work} \\ \text{=} \\ \text{Energy} \end{array}$$

$$1 \text{ V} = 1 \text{ Joule/Coul} \quad \underline{q \Delta V}$$

$$|q| = |e| \quad q_{e^-} = -1.6 \times 10^{-19} \text{ C}$$

$e^-$  gains 1 electron-Volt

$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ Joules}$$

The electron-Volt is a unit of energy that is convenient to use in science that involves small #'s of charged particles

→ Atoms, chemistry, nuclear physics